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Long-term X-ray variability of the symbiotic system RT Cru based on *Chandra* spectroscopy

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ABSTRACT

RT Cru belongs to the rare class of hard X-ray emitting symbiotics, whose origin is not yet fully understood. In this work, we have conducted a detailed spectroscopic analysis of X-ray emission from RT Cru based on observations taken by the *Chandra* Observatory using the Low Energy Transmission Grating (LETG) on the High-Resolution Camera Spectrometer (HRC-S) in 2015 and the High Energy Transmission Grating (HETG) on the Advanced CCD Imaging Spectrometer S-array (ACIS-S) in 2005. Our thermal plasma modelling of the time-averaged HRC-S/LETG spectrum suggests a mean temperature of $kT \sim 1.3$ keV, whereas $kT \sim 9.6$ keV according to the time-averaged ACIS-S/HETG. The soft thermal plasma emission component (~ 1.3 keV) found in the HRC-S is heavily obscured by dense materials ($> 5 \times 10^{23}$ cm⁻²). The aperiodic variability seen in its light curves could be due to changes in either absorbing material covering the hard X-ray source or intrinsic emission mechanism in the inner layers of the accretion disc. To understand the variability, we extracted the spectra in the 'low/hard' and 'high/soft' spectral states, which indicated higher plasma temperatures in the low/hard states of both the ACIS-S and HRC-S. The source also has a fluorescent iron emission line at 6.4 keV, likely emitted from reflection off an accretion disc or dense absorber, which was twice as bright in the HRC-S epoch compared to the ACIS-S. The soft thermal component identified in the HRC-S might be an indication of a jet that deserves further evaluations using high-resolution imaging observations.

Key words: accretion, accretion discs – binaries: symbiotic – stars: individual: (RT Cru).

1 INTRODUCTION

Symbiotic systems are interacting binary stars consisting of a hot accreting compact object and a cool red giant companion (see e.g. Allen 1984; Kenyon 1986; Kenyon & Fernandez-Castro 1987; Muerset et al. 1991; Belczyński et al. 2000). Many of them demonstrate long- and shorter-term variability (Houk 1963; Mikolajewski, Mikolajewska & Khudiakova 1990; Sokoloski, Bildsten & Ho 2001; Sokoloski 2003; Hinkle, Fekel & Joyce 2009). Although symbiotic stars mostly display soft or supersoft X-ray emission (see e.g. Muerset, Wolff & Jordan 1997), a few of them show hard X-ray emission, namely RT Cru (Luna & Sokoloski 2007; Kennea et al. 2009; Eze 2014; Ducci et al. 2016; Luna et al. 2018), CH Cyg (Kennea et al. 2009; Eze 2014), TCrB (Tueller et al. 2005; Luna, Sokoloski & Mukai 2008; Kennea et al. 2009; Eze 2014), CD-57 3057 (SS73 17) (Smith et al. 2008; Kennea et al. 2009; Eze, Luna & Smith 2010; Eze 2014), and MWC 560 (Stute & Sahai 2009). These hard X-ray emitting symbiotic systems pose a challenge to our understanding of accreting white dwarfs (WDs). We have not yet clearly understood the origin of hard X-ray emitting symbiotics. It was argued that hard X-ray emission could be an indication of massive WDs (Luna & Sokoloski 2007). Moreover, Kennea et al. (2009) proposed that these hard X-ray emitting symbiotics with massive WDs could be potentially progenitors of type Ia supernovae.

RT Cru was first classified as a symbiotic star by Cieslinski, Elizalde & Steiner (1994) based on its optical light curve features. Previously, it was identified as a visible star (Leavitt & Pickering 1906; Dunér, Hartwig & Müller 1911), a L-type variable star (Kukarkin et al. 1969), and an early (O-A) type irregular variable star (Kholopov 1987). It was observed to contain rapid brightness variations with scales of 10-30 min, so-called flickering (Cieslinski et al. 1994). It was also found that it has the hard X-rays emission using the IBIS (Imager on Board the INTEGRAL Satellite) instrument of the International Gamma-Ray Astrophysics Laboratory (INTEGRAL) satellite in 2003 and 2004 (Chernyakova et al. 2005), and again in 2012 and 2015 (Sguera et al. 2012; Sguera, Bird & Sidoli 2015). The X-Ray Telescope (XRT) on the *Swift* satellite also confirmed the presence of hard X-ray emission from its accreting WD, while also showing a large variation in X-ray flux of a factor of 3 over a period of 5 d (Kennea et al. 2009). More recently, NuSTAR observations of RT Cru pointed to a reflection in the hard X-ray spectrum from the boundary layer of the accretion disc (Luna et al. 2018).

Several X-ray observations of RT Cru revealed the presence of high plasma temperatures associated with hard X-ray emission. Using *Chandra* observations (0.3–8 keV), Luna & Sokoloski (2007) determined a plasma temperature of $kT = 8.6^{+3.8}_{-2.5}$ keV from a highly absorbed, optically thin thermal plasma model, and a temperature of $kT_{\rm max} = 80^{+...}_{-2.4}$ keV by fitting a cooling flow model with absorbers. Moreover, Kennea et al. (2009) derived $kT = 37^{+7}_{-6}$ keV with a partially covered absorbed thermal bremsstrahlung model from

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combined the Burst Alert Telescope (BAT) and X-ray telescope (XRT) on the *Swift* satellite. A *Suzaku* observation of RT Cru was also modelled with a thermal bremsstrahlung continuum having a temperature of $kT = 29^{+9}_{-5}\,\text{keV}$ (Eze 2014). Furthermore, a high cooling flow temperature of $kT_{\text{max}} = 51^{+3}_{-2}\,\text{keV}$ was estimated from combined archival *INTEGRAL* gamma-ray satellite and *Swift/XRT* data, in addition to $kT_{\text{max}} = 79.9^{+\cdots}_{-19.9}\,\text{keV}$ from *Suzaku* data (Ducci et al. 2016). More recently, Luna et al. (2018) obtained a maximum post-shock temperature of $kT = 53 \pm 4\,\text{keV}$ from spectral fitting analysis of *Suzaku* and *NuSTAR+Swift* observations, and suggested a WD mass of $1.25 \pm 0.02\,\text{M}_{\odot}$.

Previous X-ray observations of RT Cru have effectively measured its spectral features in the hard X-ray excess (>1 keV), except for the recent *Chandra* observations in 2015 that we analyse here. The X-ray observations prior to 2012 implied that RT Cru has X-ray emission produced by plasmas having high temperatures (kT > 9 keV). However, our observations in 2012 taken simultaneously by the Chandra high-resolution camera imager (HRC-I) and Swift/XRT indicated the presence of flare-like variations in the soft band below 4 keV, in addition to a possible soft thermal plasma component by Chandra/HRC-I and an anticorrelation between the intensity and spectral hardness by Swift/XRT (Kashyap et al. 2013). The flare-like variations have been detected previously (Luna & Sokoloski 2007; Kennea et al. 2009), and again recently by Ducci et al. (2016). Our knowledge of RT Cru was therefore limited to its X-ray features in the hard X-ray domain and flare-like variations prior to its recent Chandra spectroscopy.

In this study, we conducted new spectral analysis of Chandra spectroscopic observations of RT Cru taken in 2005 and 2015. The first Chandra spectroscopic observation in 2005 was taken using the Advanced CCD Imaging Spectrometer S-array (ACIS-S) with the High Energy Transmission Grating (HETG; see Section 2.2) that was more sensitive in the 'hard band' above 4 keV. The recent Chandra observations in 2015 allowed us to have a new look into the Xray characteristics of this peculiar symbiotic star after 10 yr with the same space telescope, but the High-Resolution Camera Spectrometer (HRC-S) with the Low Energy Transmission Grating (LETG; see Section 2.1) that are more sensitive in the 'soft band' below 4 keV. We used these observations in two different epochs to determine the plasma temperatures and absorbing column densities in the soft and hard energy bands, and low/hard and high/soft spectral states, as well as the mass-accretion rates in different epochs and states. In Section 2, we describe the observations and data reduction. Section 3 presents the timing and hardness ratio analyses, followed by the spectral analysis and modelling results. A discussion is presented in Section 4, and a conclusion is given in Section 5.

2 OBSERVATIONS AND DATA REDUCTION

X-ray spectroscopic observations of RT Cru were taken by the Chandra Observatory using the ACIS-S (Garmire et al. 2003) in 2005 and the HRC-S (Murray et al. 1997) in 2015. The ACIS-S observation was previously analysed by Luna & Sokoloski (2007). In our study, we employed a Markov chain Monte Carlo (MCMC) based Bayesian statistic method to determine the best-fitted parameters in our spectral modelling (see Section 3.3), and a novel approach to study the HRC-S data by decomposing the observational events according to the low/hard and high/soft spectral states (see Section 3.2) by building Good Time Interval (GTI) tables for the data reduction described in this section. We utilized the same method and approach to further study the ACIS-S data that were not implemented previously by Luna & Sokoloski (2007).

2.1 HRC-S/LETG data reduction

RT Cru was observed over two visits (Proposal 16300574, Obs.ID 16688 & 18710, PI: Karovska) during 2015 November 23–24 with the LETG (Brinkman et al. 2000) on the HRC-S. The observation details are given in Table 1. Useful exposure times of 25.15 and 53.73 ks were obtained for the two visits, respectively, which yield a total exposure time of about 79 ks over a period of \sim 1.5 d.

The data reduction was performed according to standard procedures using the software package CIAO v4.12 'Chandra Interactive Analysis of Observation' (Fruscione et al. 2006) and the calibration files from CALDB v4.9.1. All events were manually processed using the CIAO functions. The dispersed $(m=\pm 1)$ source spectra were extracted using the CIAO tools tgextract and dmtype2split. The background spectra were also produced using the tg_bkg script. The response matrix function (RMF) and the ancillary response matrix (ARF) files of the first-orders $(m=\pm 1)$ were generated using the tool mktgresp.

For the hardness ratio analysis, the CIAO function dmcopy was used to filter the level 1 (L1) events (reprocessed by hrc_process_events) based on GTI tables made for the high/soft and low/hard states (see Section 3.2), while the dead time correction factor, the exposure time, and the live time (that excludes the dead time associated with the image transfer) were manually corrected in the header keywords of the event files during the standard reduction after the event filtering procedure (see 'CIAO Manual: LETG/HRC-S Grating Spectra'2). The grating events were manually assigned to spectral orders using the CIAO function tq_resolve_events, and the source pha files were then extracted from the event files using the CIAO tool tgextract. To have high signal-to-noise ratios in the time-averaged analysis, we used the CIAO tool combine_grating_spectra to merge the dispersed spectra orders from the two observations. To produce the low/hard- and high/soft-state spectra, we similarly merged the dispersed spectra from events filtered based on GTI tables.

2.2 ACIS-S/HETG data reduction

RT Cru was observed on 2005 October 19 (Proposal 07300767, Obs.ID 7186, PI: Sokoloski) with the HETG (Weisskopf et al. 2002; Canizares et al. 2005) on the ACIS-S. The observation details are presented in Table 1. The useful exposure time was about 49 ks. The HETG instrument has two sets of gratings: the medium energy grating (MEG) and the high energy grating (HEG). The MEG covers 0.4–7 keV with a full-width at half maximum (FWHM) of 0.023 Å, whereas the HEG covers 0.8–10 keV with an FWHM of 0.012 Å (see 'Chandra Proposers' Observatory Guide' Rev.22.0, 2019). The MEG with a resolving power of $E/\Delta E = 660$ at 0.826 keV can effectively measure the soft band, while the HEG with a resolving power of $E/\Delta E = 1000$ at 1 keV was designed to be more efficient in the hard band.

We reprocessed the ACIS-S/HETG data of RT Cru with the recent calibration data (CALDB v4.9.1), and manually applied the CIAO standard functions to the HETG data to generate the plus and minus first-order ($m=\pm 1$) MEG and HEG data and their corresponding response files. We used the CIAO task tgextact to extract the pulse height amplitude (pha) files from the MEG and HEG $m=\pm 1$ orders, and the CIAO task mkgrmf and mkgarf to produce the redistribution matrix (rmf) and auxiliary response (arf) files.

¹https://cxc.harvard.edu/ciao/

²https://cxc.cfa.harvard.edu/ciao/threads/spectra_letghrcs

Table 1. Chandra Observations of RT Cru.

Instrument	Gratings	Seq. no.	Obs. ID & PI	UT start	UT end	Time (ks)
HRC-S	LETG	300332	16688, Karovska	2015 Nov 23, 02:01	2015 Nov 23, 09:38	25.15
HRC-S	LETG	300332	18710, Karovska	2015 Nov 23, 22:42	2015 Nov 24, 14:13	53.73
ACIS-S	HETG	300171	7186, Sokoloski	2005 Oct 19, 10:21	2005 Oct 20, 16:31	49.34

To implement our hardness ratio analysis, we employed the CIAO function dmcopy to copy events from the L1-event file (reprocessed by acis_process_events) based on a GTI table made for each state (high/soft and low/hard states defined in Section 3.2). We then reprocessed the copied L1-event file with the CIAO standard functions (tg_resolve_events and tgextract) to create the pha file. We merged the $m=\pm 1$ order MEG and HEG data using the CIAO tool combine_grating_spectra to make the time-averaged spectrum, low/hard-state and high/soft-stat spectra.

3 DATA ANALYSIS AND RESULTS

3.1 Light curves

To investigate the variability and hardness ratios of RT Cru during the HRC-S/LETG observations in 2015, we utilized the CIAO tool dmextract to create light curves in different energy bands and with different binning. For these hardness ratios, we chose the soft band (S: 0.3–4 keV) and the hard band (H: 4–8 keV). We binned the time series at 60 and 600 s intervals in order to detect any flickering variations and possible periodic brightness modulations of binary orbital periods or WD rotation periods. We used the tools efsearch and powspec from XRONOS timing analysis software package v5.22 (Stella & Angelini 1992) to search for periodic modulations in the light curves binned at 60 s in different energy bands. Although the light curves show aperiodic flickering variations, we did not detect any periodic modulations. This agrees with the previous studies (Luna & Sokoloski 2007; Kennea et al. 2009; Ducci et al. 2016). We used the HRC-S/LETG light curves binned at 600 s for our hardness ratio analysis, and to create GTI tables for filtering observational events according to the HR diagrams (shown in Fig. 3).

Fig. 1 shows the HRC-S/LETG light curves of RT Cru binned at 600-s intervals in the 0.3–8 keV energy band (S + H), whereas the S band (0.3–4 keV) and the H band (4–8 keV). The light curves present the net counts and were background subtracted. We notice that the light curves are dominated by the background noise in several intervals, so it was necessary to carefully handle both, the source and background, as different data sets and simultaneously model both of them in the spectral analysis. In Fig. 1, we also plotted the hardness ratios HR₁ and HR₂ described in Section 3.2. The binned light-curve points plotted by blue squares and red triangles are according to the *low/hard* and *high/soft* spectral states classified on the HR diagrams in Section 3.2, respectively.

To analyse the hardness ratios of the ACIS-S/HETG observation of RT Cru in 2005, we also employed the 'ACIS Grating Light Curve' (aglc) program³ developed by Huenemoerder et al. (2011) in the 'Interactive Spectral Interpretation System'⁴ (ISIS; Houck & Denicola 2000) to generate the light curves in 60-s and 600-s bins for three bands: the soft band (S: 0.3–4 keV), the hard band (H: 4–8 keV), and 0.3–8 keV broad-band (S + H: 0.3–8.0 keV). We did not detect

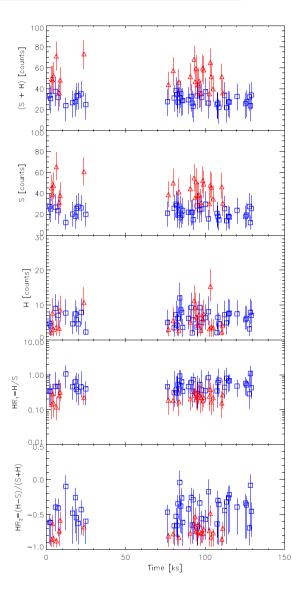


Figure 1. From top to bottom: the HRC-S/LETG light curves of RT Cru binned at 600 s in the 0.3–8 keV broad-band (S+H), 0.3–4 keV energy (S), 4–8 keV energy (H), and the hardness ratios $HR_1=H/S$ and $HR_2=(H-S)/(S+H)$, obtained from the source and background light curves using the BEHR. The time unit is kilosecond (starts at 2015-11-23 02:01). The energy band unit is counts. Plots show only bins with both statistically significant S and S and S bands. The X-ray source denoted by blue squares and red triangles are classified under the low/hard and high/soft states, respectively (see Fig. 3).

any periodic modulations in the light curves binned at 60 s. The ACIS-S/HETG light curves binned at 600 s were used to conduct the hardness ratio analysis and generate GTI tables for separating observational events according to the low/hard and high/soft spectral states in the HR diagrams (see Fig. 4).

³http://space.mit.edu/cxc/analysis/aglc/

⁴http://space.mit.edu/asc/isis/

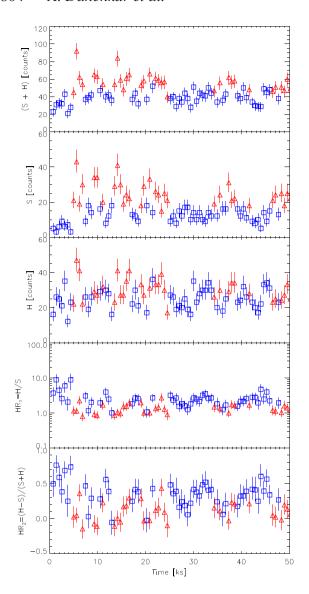


Figure 2. The same as Fig. 1, but for the ACIS-S/HETG light curves of RT Cru with a bin size of $600 \, \text{s}$. The hardness ratios HR_1 and HR_2 were derived from the source light curves using the BEHR.

In Fig. 2, we plotted the light curves of RT Cru derived from the ACIS-S/HETG data with a bin size of 600 s for the broad S+H energy band (0.3–8 keV), the S band (0.3–4 keV), and the H band (4–8 keV). The light curve units are in counts. The ACIS-S, in contrast to the HRC-S, has a negligible background noise in extracted spectra for the exposures analysed here. Fig. 2 also shows the hardness ratios HR₁ and HR₂ defined in Section 3.2. Similarly, we also plotted the binned light curves in the low/hard and high/soft states according to the HR diagrams (see Section 3.2) using blue squares and red triangles, respectively.

3.2 Hardness ratios

We conducted the hardness ratio analysis based on the light curves binned at 600 s extracted from the soft and hard energy bands. Similar hardness ratio studies of RT Cru have been carried out by Kennea et al. (2009), Ducci et al. (2016), and Luna et al. (2018). Hardness ratio spectral analyses have been also used to separate the soft thermal

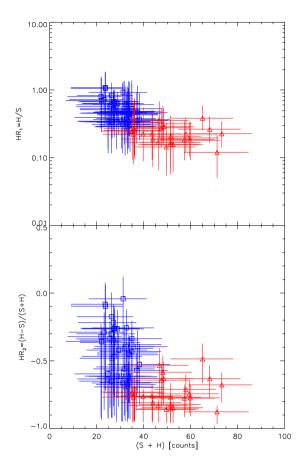


Figure 3. Hardness ratio diagrams of the HRC-S/LETG data: the hardness ratios $HR_1 = H/S$ (top panel), and $HR_2 = (H-S)/(S+H)$ (bottom panel) plotted against the energy band 0.3–8 keV (S+H; in counts) binned at 600 s. The hardness ratios were calculated using the BEHR from the source and background light curves. The X-ray source in the *low/hard* and *high/soft* states is denoted by blue squares and red triangles, respectively. Plots show only bins with both statistically significant S and H bands.

components and the hard non-thermal components in *Chandra* X-ray surveys (see e.g. Brassington et al. 2008; Plucinsky et al. 2008), as well as X-ray studies of active galactic nuclei (e.g. Worrall et al. 2010; Danehkar et al. 2018).

We calculated the hardness ratios (HR₁ and HR₂) using the following definitions and the light-curves binned at $600 \, \text{s}$ in the *soft* ($S: 0.3-4 \, \text{keV}$) and $hard \, (H: 4-8 \, \text{keV})$ bands:

$$HR_1 = H/S, \tag{1}$$

$$HR_2 = (H - S)/(S + H).$$
 (2)

To propagate uncertainties of the source and background counts, we employed the Bayesian Estimator for Hardness Ratios (BEHR; Park et al. 2006).

The hardness ratios HR_1 and HR_2 of the HRC-S/LETG light curves binned at 600-s intervals are shown in Fig. 1 (two bottom panels). For the HRC-S/LETG observations, we also plotted the hardness ratios HR_1 and HR_2 versus the 0.3–8 keV energy band (H+S) in Fig. 3. It is seen that there is an anticorrelation between the hardness ratio HR_1 and the brightness, which is in agreement with Kennea et al. (2009), Kashyap et al. (2013), and Ducci et al. (2016). The light curves shown in Fig. 1 were also classified under the *low* (hard) and *high* (soft) states based on the HR_2 versus S+H diagram of Fig. 3. The division

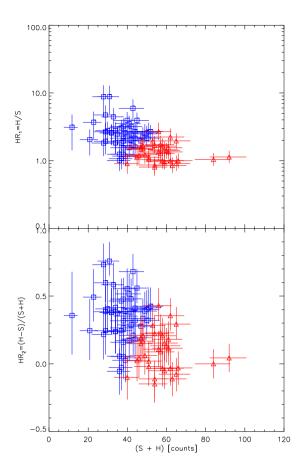


Figure 4. The same as Fig. 3, but for the ACIS-S/HETG data.

in the HR diagrams of the HRC-S/LETG data was selected according to $\mathrm{HR}_2=0.025(S+H)-1.54$ that yields an approximately equal total net counts in each state (low and high). Similarly, we divided the HR diagrams of the ACIS-S/HETG data based on $\mathrm{HR}_2=0.025(S+H)-0.96$ that provides roughly equal total net counts in the low/hard and high/soft states (see Fig. 4). The S band light curves of the HRC-S/LETG demonstrate that the X-ray source in the high/soft state emerges as approximately hourly aperiodic flickering (brightening) events. However, these brightening events were also visible in the H band light curves of the ACIS-S/HETG, in addition to those in its S band. In Figs 3 and 4, we plotted the low/hard and high/soft state events by blue squares and red triangles, respectively.

3.3 Spectral analysis

The boundary layer of an accretion disc could be optically thin or thick to its X-ray radiation in different regions, while obscuring clumpy materials moving within the line of sight around the X-ray source are thought to produce X-ray variations in RT Cru (Kennea et al. 2009). The low/hard (high/soft) state that is associated with lower (higher) brightening events could originate from either the thermal variability in the accretion flows or obscuring clumpy medium. To understand better the X-ray variability of RT Cru, we therefore modelled the spectra using a thermal plasma model covered by a local absorber that could produce X-ray variations made by obscuring clumpy materials.

We conducted the spectral analysis on the time-averaged spectra of the merged HRC-S/LETG observations and the simultaneous spectral fitting of the MEG and HEG $m=\pm 1$ orders of the

ACIS-S/HETG data. We used the CXC's Modelling and Fitting Package Sherpa⁵ (Freeman, Doe & Siemiginowska 2001), from CIAO v4.12, running under PYTHON v3.5.4, together with XSPEC X-ray spectral-fitting models (Arnaud 1996). The time-averaged spectrum analysis allowed us to study the overall physical properties of this X-ray source without considering them in the low/hard to high/soft states. To model the background in each data set, we employed an unabsorbed broken power-law component (XSPEC model bknpower) without setting any auxiliary matrix over the 0.3–8 keV energy range. For the background modelling, we used the 'cstat' statistic maximum-likelihood function (Cash 1979), together with the Levenberg-Marquardt optimization method (Moré 1978). As seen in Table 2, the power-law indexes and normalization factors of the background models are roughly similar in the HRC-S timeaveraged, low/hard-state, and high/soft-state spectra. For the ACIS-S observations (see Table 3), the backgrounds are not as high as those in the HRC-S. It can be noticed that the normalization factors and the power-law indexes of the HRC-S background models in the time-averaged, low/hard-state, and high/soft-state spectra are similar to each other. We then fixed the broken power-law model of the background spectrum, and we fitted the source spectrum for each data set. As seen in Figs 3 and 4, there are hardness-brightness anticorrelations in both the HRC-S and ACIS-S observations due to some brightness changes on hour timescales mostly in the soft excess below 4 keV. To exclude any effect of the soft band variations on our fitting, we first constructed a phenomenological model of the hard band (4–8 keV) in Section 3.3.1, and then extended our fitting model to the soft band (0.3–4 keV) in Section 3.3.2.

We conducted the 'Bayesian Low-Count X-ray Spectral Analysis in Python'⁶ (pyBLoCXS; van Dyk et al. 2001; Protassov et al. 2002; Lee et al. 2011; Xu et al. 2014) that yielded the best-fitting parameters with their corresponding uncertainties using an MCMCbased algorithm. The sampler and random walker method chosen in the pyBLoCXS analysis was the Metropolis and Metropolis-Hastings (MetropolisMH) algorithm (Metropolis et al. 1953; Hastings 1970). For our MCMC fitting, we utilized the 'Cash' Poisson logarithmlikelihood function (Cash 1979), together with the Nelder-Mead Simplex optimization method (Lagarias et al. 1998; Wright 1996). We ran 20 000 iterations to produce the MCMC chain in each spectral modelling case. The posterior probability distributions of the bestfitted parameters were extracted from the MCMC chain, which were also plotted in multidimensional projected 2D histograms together with probability density function (PDF) plots using the PYTHON module corner (Foreman-Mackey 2016).7

3.3.1 Hard excess and iron lines above 4 keV

To model the hard excess, we considered the combined first-order $(m=\pm 1)$, time-averaged spectrum in the 4–8 keV energy region. To model the continuum, we initially used a fully absorbed power-law component, implemented by using the XSPEC model phabs \times powerlaw that describes X-ray hard non-thermal emission of the accretion disc (powerlaw) and local absorption from possible moving dense material along the line of sight partially covering the source (pcfabs). As the soft excess is highly variable, we matched

⁵https://cxc.cfa.harvard.edu/sherpa/

⁶https://hea-www.harvard.edu/AstroStat/pyBLoCXS/

⁷The module corner uses the Python packages matplotlib (Hunter 2007) and numpy (van der Walt, Colbert & Varoquaux 2011; Harris et al. 2020).

Table 2. Partially covered absorbed power law and thermal modelling of the HRC-S/LETG data.

	Component	Parameter	Time averaged	Low/hard state	High/soft state	
		Source: $phabs(Hi)^a \times (pcfabs \times mekal + pcfabs \times powerlaw + \sum gauss)$				
		cstat/dof	1.03	1.09	1.08	
Soft excess	$phabs(HI)^a$	$N_{\rm H}({\rm cm}^{-2})$	1.8×10^{21}	1.8×10^{21}	1.8×10^{21}	
	phabs	$N_{\rm H, mk}({\rm cm}^{-2})$	$75.88^{+17.92}_{-21.64} \times 10^{22}$	$63.08^{+17.81}_{-11.40} \times 10^{22}$	$46.65^{+12.63}_{-21.88} \times 10^{22}$	
	mekal	<i>kT</i> (keV)	$\begin{array}{c} 1.28^{+0.93}_{-0.26} \\ 0.15^{+0.40}_{-0.10} \\ 0.86^{+1.32}_{-0.72} \end{array}$	$1.53^{+0.14}_{-0.12}$	$0.57^{+0.34}_{-0.39}$	
		$A_{\mathrm{Fe}}(A_{\mathrm{Fe}_{\odot}})$	$0.15^{+0.40}_{-0.10}$	0.15	0.15	
		$K_{\rm mk}(10^{-14}{\rm cm}^{-5})^{b}\ldots$	$0.86^{+1.32}_{-0.72}$	0.86	0.86	
	$apec^c$	<i>kT</i> (keV)	$1.13^{+0.41}_{-0.23}$	$1.26^{+0.05}_{-0.05}$	$0.68^{+0.13}_{-0.33}$	
		$K_{\rm ap}(10^{-14}{\rm cm}^{-5})^{b}$	$1.57^{+2.95}_{-1.08}$	1.57	1.57	
Hard excess	pcfabs	$N_{\rm H, p}({\rm cm}^{-2})$	$4.47^{+0.70}_{-0.51} \times 10^{22}$	$5.42^{+1.03}_{-1.04} \times 10^{22}$	$7.35^{+1.74}_{-1.44}\times10^{22}$	
		f_{p}	$0.83^{+0.02}_{-0.02}$	$0.93^{+0.01}_{-0.02}$	$0.78^{+0.03}_{-0.04}$	
	powerlaw	Γ^{d}	$1.70^{+0.21}_{-0.39}$	$2.40^{+0.23}_{-0.52}$	$1.69_{-0.08}^{+0.10}$	
		$K_{\rm p}(\frac{{ m photons}}{{ m keVcm^2s}})$	$5.56^{+0.77}_{-0.56} \times 10^{-3}$	$13.65^{+3.71}_{-3.21} \times 10^{-3}$	$9.61^{+1.29}_{-1.42} \times 10^{-3}$	
Iron lines	gauss(g1)	<i>E</i> (keV)	6.379	6.379	6.379	
	(Fe K α)	$K_{g1}\left(\frac{\text{photons}}{\text{cm}^2 \text{ s}}\right) \dots$	$9.95^{+4.23}_{-2.72} \times 10^{-5}$	$12.18^{+13.35}_{-8.87} \times 10^{-5}$	$21.38^{+15.55}_{-9.58} \times 10^{-5}$	
	gauss(g2)	<i>E</i> (keV)	6.693	6.693	6.693	
	(Fe XXV)	$K_{g2}\left(\frac{\text{photons}}{\text{cm}^2 \text{ s}}\right) \dots$	$4.82^{+3.77}_{-2.42} \times 10^{-5}$	$12.24^{+17.09}_{-7.69} \times 10^{-5}$	$13.28^{+10.11}_{-10.24} \times 10^{-5}$	
	gauss(g3)	<i>E</i> (keV)	6.946	6.946	6.946	
	(Fe XXVI)	$K_{\rm g3}\left(\frac{\rm photons}{{ m cm}^2~{ m s}}\right)$	$5.70^{+3.58}_{-3.27} \times 10^{-5}$	$22.46^{+22.31}_{-15.04} \times 10^{-5}$	$13.28^{+10.11}_{-10.24} \times 10^{-5}$	
	g1-3 ^e	$\sigma_{g1, 2, 3}(eV) \dots$	$38.08^{+103.49}_{-24.99}$	$472.99^{+119.48}_{-224.38}$	$169.98^{+182.81}_{-100.17}$	
		$F_{0.3-8}({\rm ergss^{-1}cm^{-2}})^f$	$23.2^{+0.5}_{-0.4} \times 10^{-12}$	$29.0^{+0.2}_{-0.2} \times 10^{-12}$	$32.9^{+0.4}_{-0.4} \times 10^{-12}$	
		$L_{0.3-8}({\rm ergss^{-1}})^g$	$219.3^{+1.8}_{-2.0}\times10^{33}$	$247.3^{+10.8}_{-9.3} \times 10^{33}$	$173.0^{+3.2}_{-2.7} \times 10^{33}$	
		Background: bknpower				
		cstat/dof	1.03	1.01	1.01	
	bknpower	Γ_1	$1.88^{+0.01}_{-0.05}$	$1.87^{+0.02}_{-0.05}$	$1.88^{+0.03}_{-0.01}$	
		$E_{\text{break}}(\text{keV})$	$3.10^{+1.45}_{-2.02}$	$2.77_{-1.75}^{+1.44}$	$2.89_{-2.89}^{+1.22}$	
		Γ_2	$2.01^{+0.21}_{-0.10}$	$2.01_{-0.10}^{+0.17}$	$1.98^{+0.08}_{-0.07}$	
		$K\left(\frac{\text{photons}}{\text{keV cm}^2 \text{ s}}\right) \dots$		$69.80^{+2.87}_{-0.10} \times 10^{-2}$	$68.64^{+0.53}_{-68.64} \times 10^{-2}$	

Note. The uncertainties of the fitted parameters are at 68 per cent confidence. The fully absorbed thermal plasma model was fitted to the low/hard- and high/soft-state spectra assuming the metal abundance $A_{\rm Fe}$ and normalization factors $K_{\rm mk}$ and $K_{\rm ap}$ derived from the time-averaged spectrum. $^a{\rm The}$ Galactic H1 foreground absorption. $^b{\rm Normalization}$ unit in $(10^{-14}/4\pi D^2)\int n_{\rm e}n_{\rm H} {\rm dV}$, where $D({\rm cm})$ is the angular diameter distance, $n_{\rm e}({\rm cm}^{-3})$ is the electron density, $n_{\rm H}$ is the hydrogen density, and V is the volume. $^c{\rm The}$ apec model substituted for the mekal model was constrained by adopting all the parameters determined from the absorbed thermal plasma model plus the partially absorbed powerlaw and gauss models, and assuming the same metal abundance $A_{\rm Fe}$ found by the mekal model. The model made with apec yields the same cstat/dof. $^d{\rm The}$ power-law index Γ is associated with the phenomenological model that describes the continuum over the 4–8 keV energy range. $^e{\rm The}$ Fe XXV and Fe XXVI line widths were linked to the Fe K α line width (having higher count rates). $^f{\rm The}$ absorbed X-ray flux over the 0.3–8 keV energy band ($D=1.64\,{\rm kpc}$).

the absorbed power-law model to the spectrum above 4 keV. Three Gaussian components (XSPEC model gauss) were also included at 6.379, 6.693, and 6.946 keV (at the rest frame, they are not redshifted or blueshifted), which could be associated with the Fe K α , Fe XXV, and Fe XXVI lines, respectively. Fig. 5 shows the iron lines in the timeaveraged spectra of HRC-S and ACIS-S (MEG and HEG gratings). It can be seen that the Fe K α are stronger than the Fe XXV and Fe XXVI lines. As the Fe xxv and Fe xxvI lines in both the HRC-S and ACIS-S spectra had insufficient count rates for constraining their upper and lower uncertainties using our MCMC-based method, we linked their line widths to the line width (σ in Tables 2 and 3) of the Fe K α line with higher count rates in our spectral fitting analysis (using the link function in Sherpa). However, the equivalent widths of the Fe XXV and Fe XXVI lines were reported to be lower than that of the Fe K α line (Eze 2014). To achieve a better fit, we then used a power-law component partially covered by an absorption model, so the phenomenological model of the hard excess (4–8 keV) with iron lines is pcfabs \times powerlaw + \sum gauss.

Using the Levenberg–Marquardt optimization method and cstat maximum-likelihood function (without pyBLoCXS), the fully absorbed power-law modelling (phabs × powerlaw) of the HRC-S/LETG time-averaged spectrum yielded a photon index of $\Gamma=1.84^{+0.06}_{-0.06}$. Similarly, for the combined MEG and HEG fitting of the ACIS-S first-order ($m=\pm 1$) data we found $1.27^{+0.45}_{-0.42}$, which roughly agrees with $\Gamma=1.05^{+0.24}_{-0.27}$ found by Luna & Sokoloski (2007). For the absorption component, we also obtained absorbing column densities $N_{\rm H}=15\pm 6\times 10^{22}\,{\rm cm}^{-2}$ for the HRC-S data and $N_{\rm H}=22\pm 7\times 10^{22}\,{\rm cm}^{-2}$ for ACIS-S data, which are higher than $N_{\rm H}=7\pm 1\times 10^{22}\,{\rm cm}^{-2}$ found by Luna & Sokoloski (2007). Using the Nelder–Mead Simplex optimization method and Cash logarithm-likelihood function (with pyBLoCXS), the best-fitting model of the HRC-S time-averaged data with a partially covered absorbed

Table 3. The same as Table 2, but for the ACIS-S/HETG data.

	Component	Parameter	Time averaged	Low/hard state	High/soft state	
		$Source: phabs(HI) \times (phabs \times mekal + pcfabs \times powerlaw + \sum gauss)$				
		cstat/dof	0.31	0.14	0.15	
Soft excess	phabs(HI)	$N_{\rm H}({\rm cm}^{-2})$	1.8×10^{21}	1.8×10^{21}	1.8×10^{21}	
	phabs	$N_{\rm H, mk}({\rm cm}^{-2})$	$12.44^{+0.71}_{-0.84} \times 10^{22}$	$7.56^{+1.38}_{-1.09} \times 10^{22}$	$12.33^{+1.67}_{-1.83} \times 10^{22}$	
	mekal	<i>kT</i> (keV)	$9.64^{+2.69}_{-3.96}$	$45.86^{+12.74}_{-17.48}$	$4.37^{+2.25}_{-2.38}$	
		$A_{\mathrm{Fe}}(A_{\mathrm{Fe}_{\odot}})$	$0.31^{+1.96}_{-0.31}$	0.31	0.31	
		$K_{\rm mk}(10^{-14}{\rm cm}^{-5})$	$1.62^{+0.13}_{-0.17} \times 10^{-2}$	$0.59^{+0.21}_{-0.16} \times 10^{-2}$	$2.06^{+1.28}_{-0.45} \times 10^{-2}$	
	apec	<i>kT</i> (keV)	$10.25^{+5.11}_{-1.35}$	$50.94^{+}_{-41.70}$	$3.81^{+1.36}_{-0.78}$	
		$K_{\rm ap}(10^{-14}{\rm cm}^{-5})\dots$	$1.59^{+0.05}_{-0.06} \times 10^{-2}$	$0.61^{+0.09}_{-0.14} \times 10^{-2}$	$2.32^{+0.46}_{-0.39}\times10^{-2}$	
Hard excess	pcfabs	$N_{\rm H, p}({\rm cm}^{-2})$	$105.27^{+46.08}_{-46.47}\times10^{22}$	$30.77^{+5.22}_{-4.96} \times 10^{22}$	$43.28^{+12.52}_{-19.62} \times 10^{22}$	
		f_{p}	1.00	1.00	$0.98^{+0.01}_{-0.01}$	
	powerlaw	Γ	$1.79^{+0.17}_{-0.21}$	$2.04^{+0.23}_{-0.24}$	$0.92^{+0.39}_{-0.15}$	
		$K_{\rm p}\left(\frac{{ m photons}}{{ m keVcm^2s}}\right)$	$15.68^{+11.79}_{-5.68}\times10^{-3}$	$10.20^{+2.50}_{-2.63}\times10^{-3}$	$1.88^{+0.89}_{-0.50} \times 10^{-3}$	
Iron lines	gauss(g1)	<i>E</i> (keV)	6.379	6.379	6.379	
	(Fe K α)	$K_{g1}\left(\frac{\text{photons}}{\text{cm}^2\text{ s}}\right)$	$4.60^{+0.99}_{-0.95} \times 10^{-5}$	$10.46^{+3.42}_{-2.61} \times 10^{-5}$	$5.30^{+2.56}_{-2.14} \times 10^{-5}$	
	gauss(g2)	E(keV)	6.693	6.693	6.693	
	(Fe XXV)	$K_{\rm g2}(\frac{\rm photons}{{ m cm}^2{ m s}})$	$3.04^{+1.09}_{-1.01} \times 10^{-5}$	$2.46^{+3.01}_{-1.56} \times 10^{-5}$	$6.91^{+3.58}_{-4.35} \times 10^{-5}$	
	gauss(g3)	E(keV)	6.946	6.946	6.946	
	(Fe XXVI)	$K_{g3}\left(\frac{\text{photons}}{\text{cm}^2 \text{ s}}\right) \dots$	$2.79^{+0.95}_{-0.93} \times 10^{-5}$	$1.43^{+2.74}_{-1.04} \times 10^{-5}$	$5.52^{+4.26}_{-3.18} \times 10^{-5}$	
	g1-3	$\sigma_{g1, 2, 3}(eV) \dots$	$38.53^{+11.23}_{-9.71}$	$71.65^{+48.32}_{-20.67}$	$174.73^{+14.85}_{-103.58}$	
		$F_{0.3-8}({\rm ergss^{-1}cm^{-2}})$	$14.5^{+0.4}_{-0.4} \times 10^{-12}$	$12.3^{+0.6}_{-1.1} \times 10^{-12}$	$16.4^{+0.9}_{-1.0} \times 10^{-12}$	
		$L_{0.3-8}(ergs s^{-1}) \dots$	$38.5^{+1.0}_{-1.4} \times 10^{33}$	$20.4^{+1.3}_{-1.1} \times 10^{33}$	$18.0^{+1.1}_{-1.1} \times 10^{33}$	
		Background: bknpower				
		cstat/dof	0.35	0.15	0.15	
	bknpower	Γ_1	$6.00^{+1.22}_{-1.05}$	$6.25^{+0.87}_{-0.89}$	$5.74_{-2.05}^{-1.54}$	
		$E_{\text{break}}(\text{keV})$	$1.37^{+0.12}_{-0.34}$	$1.38^{+0.07}_{-0.27}$	$1.45^{+0.20}_{-0.56}$	
		Γ_2	$0.71^{+1.08}_{-0.30}$	$0.44^{+0.91}_{-0.25}$	$0.84^{+1.72}_{-0.52}$	
		$K\left(\frac{\text{photons}}{\text{keV cm}^2 \text{ s}}\right) \dots$	$28.54^{+14.61}_{-12.71} \times 10^{-5}$	$27.30^{+11.48}_{-9.62} \times 10^{-5}$	$35.50^{+27.01}_{-22.78} \times 10^{-5}$	

Note. The uncertainties of the fitted parameters are at 68 per cent confidence. The background model parameters, the powerlaw photon index Γ , the gauss parameters, and the mekal metal abundance $A_{\rm Fe}$ were determined from the simultaneously fitted MEG and HEG data, while the remaining parameters were derived from the MEG spectrum. The fully absorbed thermal plasma model was fitted to the low/hard-and high/soft-state spectra assuming the metal abundance $A_{\rm Fe}$ derived from the time-averaged spectrum. The apec model parameters were obtained by fixing the parameters derived from the full model with mekal.

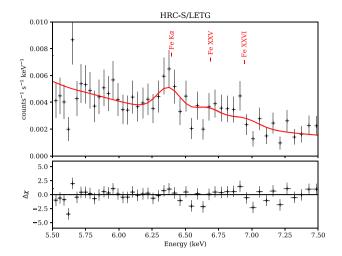
power-law component (pcfabs × powerlaw) has a power-law index $\Gamma=1.70^{+0.21}_{-0.39},$ while for the ACIS-S data $\Gamma=1.79^{+0.17}_{-0.21}.$ The best-fitting photon indexes of the partially covered absorbed power-law model and the best-fitting parameters of the three Gaussian components (pcfabs×powerlaw+ \sum gauss) obtained for the HRC-S and ACIS-S data are presented in Tables 2 and 3, respectively. These parameters were determined by restricting the spectral fitting analysis to the hard excess (4–8 keV).

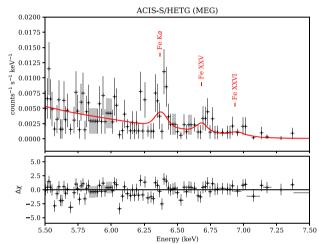
Fig. 6 shows the posterior probability distributions of the parameters plotted by the module corner for the partially absorbed power-law model with three Gaussian components simultaneously fitted to the MEG and HEG first-orders ($m=\pm 1$) of the ACIS-S/HETG time-averaged data over the hard excess (4–8 keV). The multidimensional probability distributions of the parameters for the HRC-S/LETG time-averaged data are presented in Fig. A1 in Appendix A (see Supplementary Material). These probability distributions of the model parameters were obtained from the MCMC chains built by pyBLoCXS in Sherpa. It can be seen that the power-law index and the parameters of the Gaussian components were properly fitted in both the ACIS-S and HRC-S observations, while we obtained a

much better fit for the ACIS-S data. The 68 per cent confidence uncertainties of the model parameters fitted to the HRC-S data are much higher than those derived for the ACIS-S data.

3.3.2 Extension to soft excess below 4 keV

To describe the emission from optically thin thermal plasma in the broad-band (0.3–8 keV), we included a fully absorbed XSPEC model mekal that describes a Mewe–Kaastra–Liedahl thermal plasma (Mewe, Gronenschild & van den Oord 1985; Mewe, Lemen & van den Oord 1986; Kaastra 1992; Liedahl, Osterheld & Goldstein 1995; Phillips et al. 1999) using ionization balances from Arnaud & Rothenflug (1985) and Arnaud & Raymond (1992). Moreover, we reproduced the thermal emission by replacing mekal with the apec model (Astrophysical Plasma Emission Database; Smith et al. 2001) that calculates emission spectra using the AtomDB atomic database (Smith et al. 2001; Foster et al. 2012). We matched the XSPEC models phabs × mekal to the 0.3–8 keV energy range by fixing the powerlaw index Γ and gauss parameters previously fitted to the hard energy band above 4 keV, but constraining again





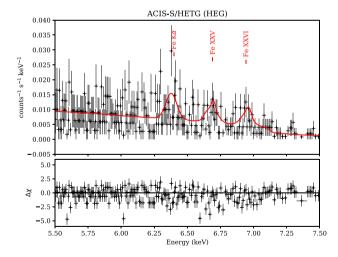


Figure 5. The Fe K α , Fe XXV, and Fe XXVI lines in the time-averaged HRC-S/LETG spectrum (top panel) and ACIS-S/HETG MEG and HEGgrating spectra (bottom panels), modelled by the Gaussian functions (XSPEC model gauss) added to the powerlaw model with the parameters listed in Tables 2 and 3, respectively. The ACIS-S MEG- and HEG-grating spectra were simultaneously fitted. The spectra are shown without any grouping scheme.

the powerlaw normalization factor K_p , as well as the pcfabs column density $N_{\rm H,\,p}$ and covering fraction $f_{\rm p}$. The thermal plasma modelling was implemented by computing the mekal model in each fitting iteration. The mekal normalization factor is defined as K_{mk} = $(10^{-14}/4\pi D^2) \int n_e n_H dV$, which is a function of the angular diameter distance D(cm), electron density $n_e(cm^{-3})$, hydrogen density $n_{\rm H}({\rm cm}^{-3})$, and gas volume V. To make the mekal normalization factor consistent with that in the apec model, we set a hydrogen density of $n_{\rm H} = 1 \, {\rm cm}^{-3}$ that is used by default in mekal. Different values of $n_{\rm H}$ result in different $K_{\rm mk}$. We should note that the number density of a dense accretion disc in the symbiotic system could be $n_{\rm H} \sim 10^8 - 10^9 \, {\rm cm}^{-3}$; however, we could not constrain $n_{\rm H}$ with the current available data. The free parameters are the plasma temperature (kT), metal abundance (A_{Fe}) , normalization factor (K_{mk}) , and absorbing column density $(N_{\rm H, mk})$ of the fully absorbed thermal model (phabs×mekal).

We adopted the ISM composition of Wilms, Allen & McCray (2000) as the baseline abundances for all the models. We determined a metal abundance of $A_{\rm Fe} = 0.15^{+0.40}_{-0.10}$ (with respect to Wilms et al.) from the initial MCMC analysis of the mekal model fitted to the time-averaged HRC-S/LETG spectrum. Although this is ostensibly smaller than the value found by Luna & Sokoloski (2007) - $A_{\rm Fe}=0.30^{+0.15}_{-0.28}$ at 1σ confidence relative to a baseline composition of Anders & Grevesse (1989) – but the uncertainty range overlap. For the ACIS-S/HETG data, we initially fitted the fully absorbed thermal plasma model simultaneously to both the MEG and HEG gratings time-averaged spectra, which provided $A_{\text{Fe}} = 0.31^{+1.96}_{-0.31}$ (at 68 per cent confidence). As the metal abundance has a high uncertainty, we fixed it to this value to conduct further the MCMCbased analysis. While the HEG grating observations allowed us to measure the iron lines in the hard band, the resulting spectrum has fewer counts in the soft band, leading to weak constraints for the mekal model. As the HEG was less efficient in the soft band (resulting in poor constraints), we excluded the HEG grating and fitted the absorbed thermal model to the MEG grating $(m = \pm 1)$ with the same values of the Gaussian parameters, power-law index Γ , and abundance $A_{\rm Fe}$ determined from the simultaneously fitted MEG and HEG data.

To account for the Galactic HI foreground absorption, we considered the total Galactic mean column density of $N_{\rm H\,I}=9.76\times$ 10^{21} cm⁻² and E(B - V) = 2.052 from the UK Swift Science Data Centre⁸ (Willingale et al. 2013). As this value corresponds to the total Galactic column density of hydrogen in the line of sight, we need to scale it based on the Galactic location of RT Cru. From the parallax of $0.6096 \pm 0.0582 \times 10^{-3}$ arcsec reported by the second *Gaia* data release (Gaia Collaboration et al. 2016; Luri et al. 2018; Gaia Collaboration et al. 2018), we derived a distance of $1.64^{+0.17}_{-0.14}$ kpc to RT Cru. Bailer-Jones et al. (2018) also estimated a distance of $1.58^{+0.17}_{-0.14}$ by correcting the parallax for the nonlinearity of the transformation. Assuming D = 1.64 kpc, we adopted $N_{\rm H\,I} = 1.8 \times 10^{21} \, \rm cm^{-2}$ that is also associated with the RT Cru interstellar extinction of E(B -V) = 0.374 measured from optical observations (Luna et al. 2018). We note that this column density can be also calculated using the empirical correlation $N(\text{H\,I})[\text{cm}^{-2}] = E(B - V)[\text{mag}] \times 4.8 \times 10^{21}$ estimated from Ly α absorption measurements (Bohlin, Savage & Drake 1978). To model the Galactic foreground absorption affecting the X-ray soft band, we employed another phabs component with the fixed parameter $N_{\rm H\,I}=1.8\times10^{21}\,{\rm cm}^{-2}$. The final phenomenological model over the broad-band (0.3-8 keV) is phabs(HI)

⁸https://www.swift.ac.uk/analysis/nhtot/

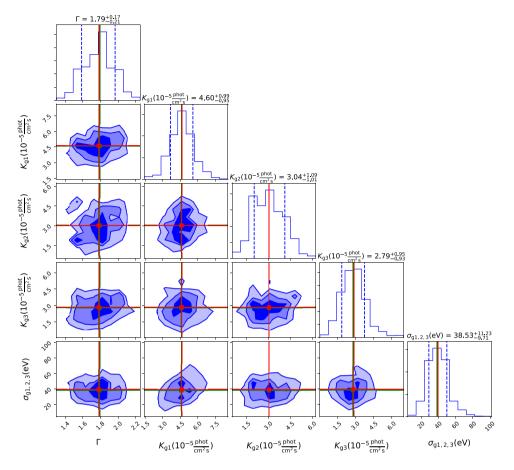


Figure 6. The posterior probability distributions of the model parameters fitted to the ACIS-S/HETG time-averaged spectrum ($m = \pm 1$ orders; MEG and HEG) over the hard excess (4–8 keV). Contours are shown at the 1σ (68 per cent), 2σ (95 per cent), and 3σ (99.7 per cent) confidence levels. The model parameters are as follows: the powerlaw index (Γ), the normalization factor (K_{g1} , K_{g2} , and K_{g3}) of the Gaussian components (XSPEC model gauss) associated with the Fe K α , Fe XXV, and Fe XXVI lines, respectively, and the line width ($\sigma_{g1,2,3}$) of the Gaussian components. The best-fitting parameters located at the true means drawn by the solid red lines are listed in Table 3. The 1σ (68 per cent) confidence levels are plotted by the dashed blue lines in the PDF plots, and the empirical means shown by the solid green lines.

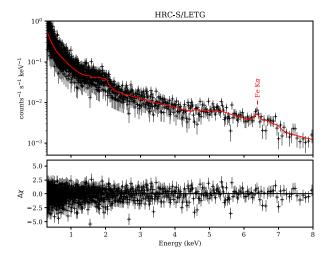
 \times (phabs \times mekal+pcfabs \times powerlaw+ \sum gauss). We plotted the best-fitted models for the time-averaged spectra of the HRC-S and ACIS-S observations in Fig. 7 along with $\Delta\chi \equiv (\text{data} - \text{model})/\text{error}$ (residuals divided by uncertainties). The spectra shown in this figure were grouped to obtain a minimum of 5 counts bin⁻¹, but our spectral fitting analysis of all the spectra was implemented without any grouping scheme.

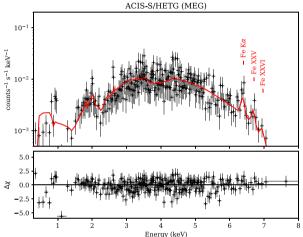
The HRC-S time-averaged spectrum was well matched to an absorbed thermal plasma model (phabs×mekal) with a plasma temperature of $kT=1.3^{+0.9}_{-0.3}\,\mathrm{keV}$ and an absorbing column density of $N_{\mathrm{H,mk}}=76^{+18}_{-22}\times10^{22}\,\mathrm{cm^{-2}}$. It can be seen that the plasma emission was heavily obstructed by the local presence of highly dense clumps within the line of sight. To include the apec model, we fixed all fitted parameters and replaced mekal with apec having the same metal abundance derived from the mekal model. It was found that the apec model fits the HRC-S spectrum with $kT=1.1^{+0.4}_{-0.2}\,\mathrm{keV}$ that is roughly the same plasma temperature derived from mekal. The parameters of the thermal plasma model fitted to the HRC-S/LETG data are listed in Table 2.

Fig. 8 shows the posterior probability distributions of the parameters of the absorbed thermal plasma model fitted together with the partially absorbed power-law model, while the power-law index Γ and the Gaussian parameters were fixed at the values found in

Section 3.3.1. As seen, there are strong constraints on the column density $(N_{\rm H,\,p})$, covering fraction $(f_{\rm p})$, and normalization factor $(K_{\rm p})$ of the partially absorbed power-law model. However, we notice extremely weak constraints on the metal abundance $(A_{\rm Fe})$ and normalization factor $(K_{\rm mk})$ of the mekal model. Although the plasma temperature (kT) is weakly constrained by the metal abundance $(A_{\rm Fe})$ and normalization factor $(K_{\rm mk})$, it is strongly restrained by the absorbing column density $(N_{\rm H,\,mk})$ of the thermal model, and the parameters of the partially absorbed power-law model. The value of the absorbing column density $N_{\rm H,mk}=76^{+18}_{-22}\times10^{22}\,{\rm cm}^{-2}$ indicates that the emission lines produced by the thermal plasma are strongly absorbed and are not easily distinguishable in the spectrum.

For the ACIS-S time-averaged MEG spectrum, the best-fitting mekal model has a plasma temperature of $kT=9.6^{+2.7}_{-4.0}$ keV, which is roughly similar to $kT=8.6^{+3.8}_{-2.5}$ keV previously derived from the ACIS-S data by Luna & Sokoloski (2007). For the fully absorbed thermal plasma model, we obtained an absorbing column density of $N_{\rm H,mk}=12.4^{+0.7}_{-0.8}\times10^{22}\,{\rm cm}^{-2}$ in reasonable agreement with $N_{\rm H}=9.3^{+3.2}_{-2.1}\times10^{22}\,{\rm cm}^{-2}$ found by Luna & Sokoloski (2007). We should note that Luna & Sokoloski (2007) did not include the second phabs component with $N_{\rm H}=0.18\times10^{22}\,{\rm cm}^{-2}$ to model the Galactic H1 foreground absorption. Moreover, we reprocessed the ACIS-S data with the most recent calibration data and the updated reduction





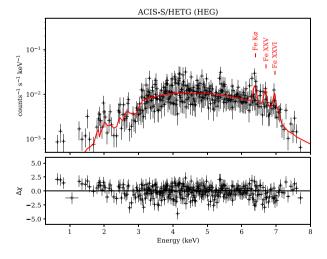


Figure 7. The dispersed $(m=\pm 1)$ time-averaged HRC-S/LETG spectrum (top panel) and the ACIS-S/HETG $(m=\pm 1)$ MEG and HEG grating spectra (bottom panels) of RT Cru. The source model is a partially covered absorbed power law plus fully absorbed thermal plasma together with Gaussian iron lines, phabs × (phabs × mekal + pcfabs × powerlaw + \sum gauss). The best-fitting parameters for the HRC-S and ACIS-S are listed in Tables 2 and 3, respectively. The plotted spectra were grouped into bins containing ≥5 counts each after the spectral fitting analysis.

package CIAO, and we still obtained similar results. The posterior probability distributions of the fitted parameters are shown in Fig. A7. Table 3 presents the best-fitting model parameters for the ACIS-S/HETG data.

3.4 Low/hard and high/soft states

The hardness–brightness anticorrelations seen in Figs 3 and 4 could be due to some flickering variations on hour timescales in the soft band. To understand the origin of such a variation, we extracted the spectra for both the low/hard and high/soft states according to criteria explained in Section 3.2. The *low/hard* and *high/soft* state events are distinguished by blue squares and red triangles in Figs 1–4, respectively. We utilized the first-order ($m=\pm 1$) spectra produced for the low/hard and high/soft states, and repeated the same spectral analysis performed for the time-averaged spectrum in Section 3.3 for both the HRC-S/LETG and ACIS-S/HETG data. The parameters of the best-fitting models for the low/hard and high/soft states are listed in Tables 2 and 3.

To produce the continuum over the 4-8 keV energy range, we used a power-law component that could be a phenomenological model. It is seen that the power-law photon index Γ is higher when the source was in the low (harder) state, which is in contrast to what we typically see for the power-law model (0.3-8 keV) fitted to the low/hard and high/soft states in X-ray binaries. We obtained $\Gamma = 2.40^{+0.23}_{-0.52}$ (low/hard state) and $\Gamma = 1.69^{+0.10}_{-0.08}$ (high/soft state) for the HRC-S data, and $\Gamma = 2.04^{+0.23}_{-0.24}$ (low/hard) and $\Gamma = 0.92^{+0.39}_{-0.15}$ (high/soft) for the ACIS-S data. The power-law normalization factor $K_{\rm p}$ of the source in the low/hard state is around 1.4 time higher than that in the high/soft state in the HRC-S observations, while K_p (low/hard) is about 5.4 time higher than K_p (high/soft) in the ACIS-S observation. The iron line measurements in the low/hard and high/soft state spectra are extremely uncertain due to lower count rates compared to the time-average spectra. We notice that the Fe K α line at 6.4 keV, which could originate from either the reflection off an accretion disc or neutral dense clumps, in the high/soft state is twice stronger than that in the low/hard state in the HRC-S observations. However, we see an opposite situation in the ACIS-S observation. Our Bayesian low-count analysis suggested that the highly ionized Ly α iron line at 6.95 keV might be stronger in the HRC-S low/hard state, while this line and the highly ionized He α iron line at 6.67 keV are likely stronger in the ACIS-S low/hard state, but with extremely high uncertainties in both the 2005 and 2015 observations. The probability distributions of the power-law index and the Gaussian parameters are shown in Figs A2–A5 (Supplementary Material). We see that the power-law continuum and the Fe K α line were strongly constrained in the ACIS-S, but weakly in the HRC-S. Moreover, we do not see any robust constraints on the Fe XXV and Fe XXVI lines, and the line widths in the low/hard- and high/soft-state spectra.

We fitted the fully absorbed thermal plasma model to the low/hard-and high/soft-state spectra of the HRC-S data by assuming $A_{\rm Fe}=0.15$ deduced from the time-averaged spectra in Section 3.3. As we could not determine the confidence level bounds of $K_{\rm mk}$ in the low/hard and high/soft states, we adopted the mekal normalization factor $K_{\rm mk}$ derived from the time-averaged HRC-S spectrum (having counts twice that in each state) to compute the covariance matrix for our MCMC statistic method. Fixing the metal abundance $A_{\rm Fe}$ and the normalization factor $K_{\rm mk}$ of the mekal model allowed us to properly constrain the confidence level bounds of other free parameters (see Figs 9 and A6). We derived a plasma temperature of $kT=1.5\pm0.1$ and $0.6^{+0.3}_{-0.4}$ keV in the low/hard and high/soft states, respectively, while $kT=1.3^{+0.4}_{-0.2}$ keV was obtained from the

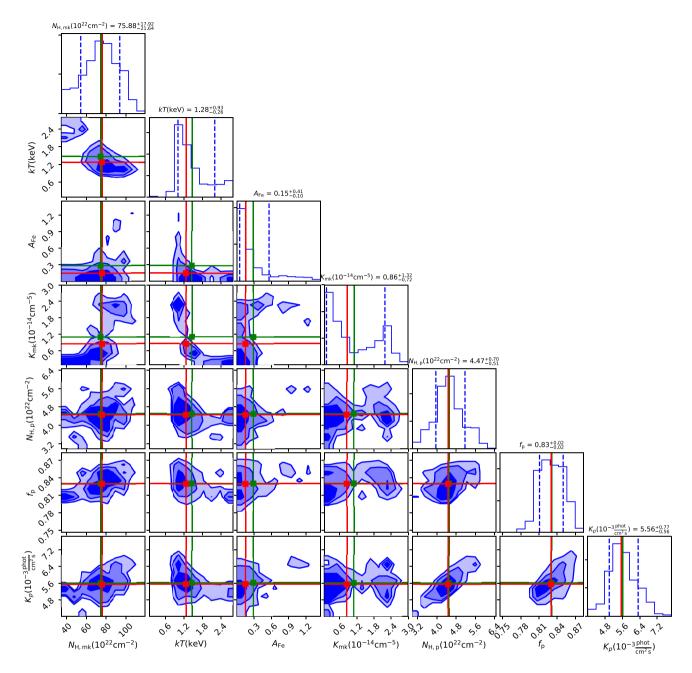


Figure 8. The posterior probability distributions of the parameters of the thermal plasma model fitted to the HRC-S/LETG time-averaged spectrum over the broad-band (0.3–8 keV). Contours are shown at the 1σ (68 per cent), 2σ (95 per cent), and 3σ (99.7 per cent) confidence levels. The model parameters are as follows: the absorbing column density ($N_{\rm H,\,mk}$), plasma temperature (kT), metal abundance ($A_{\rm Fe}$), and normalization factor ($K_{\rm mk}$) in 10^{-14} cm⁻⁵ of the thermal plasma model (phabs×mekal); and the column density ($N_{\rm H,\,p}$), covering fraction ($f_{\rm p}$), and normalization factor ($K_{\rm p}$) of the partially absorbed power-law model (pcfabs×powerlaw). The best-fitting parameters located at the true means drawn by the solid red lines are listed in Table 2. The 1σ confidence levels are plotted by the dashed blue lines in the PDF plots, and the empirical means shown by the solid green lines.

time-averaged spectrum containing both the low/hard- and high/soft-state events. Similarly, from the apec model we obtained $kT=1.3\pm0.1$ and $0.7^{+0.1}_{-0.3}$ keV for the low/hard- and high/soft-state spectra, respectively. It can be seen that the plasma was slightly hotter in the low (hard) state and cooler in the high (soft) state. As seen in Fig. 9, the probability distributions of the plasma temperature (kT) and the column density $(N_{\rm H,\,mk})$ of the fully absorbed thermal plasma model were robustly fitted together with the column density $(N_{\rm H,\,p})$, covering fraction $(f_{\rm p})$, and normalization factor $(K_{\rm p})$ of the partially absorbed power-law model in the low-/hard-state spectrum.

However, we see in Fig. A6 that our fitting analysis provided an upper limit to the plasma temperature (kT) in the high/soft state spectrum, while we obtained solid constraints on the parameters of the absorbed power-law model, but an extremely weak constraint on the absorbing column density of the thermal plasma model.

The absorbed mekal model was also fitted to the low/hard- and high/soft-state ACIS-S spectra by taking $A_{\rm Fe}=0.31$ derived from the time-averaged data in Section 3.3. We obtained $kT=4.4^{+2.3}_{-2.4}$ and $45.9^{+12.7}_{-17.5}$ keV for the high/soft- and low/hard-state spectra, respectively, while we got $kT=9.6^{+2.7}_{-4.0}$ keV from the time-averaged

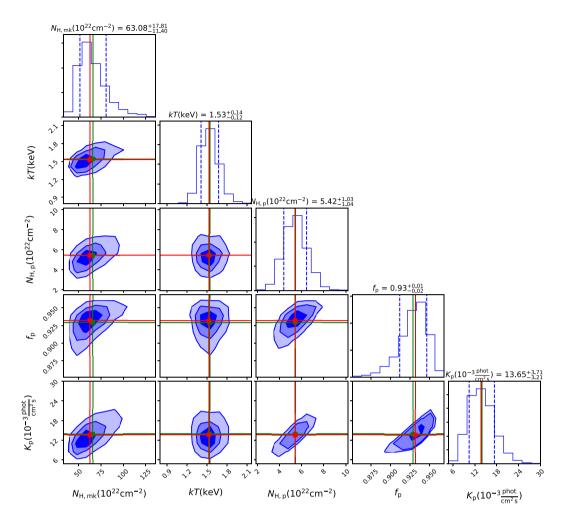


Figure 9. The same as Fig. 8, but for the HRC-S/LETG low/hard-state spectrum.

spectrum. The apec model provided $kT = 3.8^{+1.4}_{-0.8}$ and $50.9^{+...}_{-41.7}$ keV (the upper error cannot be constrained) for the high/soft- and low/hard-state spectra, respectively, which are similar to the mekal results. As the low/hard-state spectrum did not have sufficient count rates, we could not determine its upper confidence limit using the apec model. Again, similar to the HRC-S data, the thermal plasma was found to be hotter in the low/hard state and cooler in the high/soft state. However, the plasma temperatures derived from the ACIS-S/HETG data are higher than those from the HRC-S/LETG data. We should note that the ACIS-S/HETG spectrometer is more efficient in the hard band, while the HRC-S/LETG spectrometer effectively records the soft band, so the discrepancy between the ACIS-S and HRC-S results could be related to their respective sensitivity energy ranges. Alternatively, the thermal plasma in RT Cru might be hotter in 2005 in the ACIS-S epoch, and cooler in 2015 during the HRC-S observations. Figs A8 and A9 present the probability distributions of the model parameters for the low/hard- and high/soft-state ACIS-S spectra. While the plasma temperature (kT) was robustly fitted in the time-averaged ACIS-S spectrum, the probability distributions of the mekal temperature are very wide in the low/hard and high/soft states. However, the absorbing column density $(N_{\rm H, mk})$ and normalization factor (K_{mk}) of the thermal model were well fitted in all the spectra (time-averaged, low, and high). The covering fractions (f_p) of the powerlaw model are about 1.0 in all the models (fully absorbed power law) of the ACIS-S/HETG data.

4 DISCUSSION

4.1 Mass accretion rate

The accretion of gas by a WD leads to the formation of a shock front near the stellar surface that creates a hot plasma environment between the shock front and the stellar surface. The temperature of the hot plasma depends only on the WD mass, while the luminosity variability is proportioned to the accretion rate. Accordingly, Luna et al. (2018) derived a WD mass of $M_{\rm WD}=1.25~{\rm M}_{\odot}$ and a WD radius of $R_{\rm WD}=7.1\times10^8~{\rm cm}$ from a maximum post-shock temperature of 53 keV estimated from Suzaku and NuSTAR+Swift.

Following Luna & Sokoloski (2007), the mass accretion rate can be estimated from the unabsorbed *hard* X-ray luminosity L_x between 0.3 and 8 keV:

$$\dot{M} = \frac{2L_{\rm x}R_{\rm WD}}{GM_{\rm WD}}.$$
 (3)

For the L_x calculations of the HRC-S data, we did not include the *soft* thermal plasma mekal model as it originates from either the outer layer or soft flickering variation due to its high luminosity (resulting in a nonphysical mass accretion rate). As we obtained a lower limit to the hot plasma temperature in the *hard* thermal plasma mekal model in the ACIS-S data, their mass accretion rate \dot{M} and X-ray luminosity L_x approximately correspond to a lower estimation of X-ray emission produced in an inner layer of the accretion disc.

Table 4. The unabsorbed *hard* X-ray luminosity and mass-accretion rate from the HRC-S/LETG and ACIS-S/HETG data.

Parameter	Time averaged	Low/hard state	High/soft state			
HRC-S/LETG: powerlaw						
$F_{\rm x}({\rm ergs~s^{-1}~cm^{-2}})^a$	$34.90^{+0.38}_{-0.37} \times 10^{-12}$	$64.55^{+1.67}_{-1.60} \times 10^{-12}$	$60.01^{+1.33}_{-1.54} \times 10^{-12}$			
$L_{\rm X}({\rm ergss^{-1}})^a$	$11.23^{+0.12}_{-0.12} \times 10^{33}$	$20.77^{+0.51}_{-0.54} \times 10^{33}$	$19.31^{+0.43}_{-0.50} \times 10^{33}$			
$\dot{M}(\mathrm{M}_{\odot}\mathrm{yr}^{-1})^{b}$	$1.52^{+0.02}_{-0.02} \times 10^{-9}$	$2.82^{+0.07}_{-0.07} \times 10^{-9}$	$2.62^{+0.06}_{-0.07} \times 10^{-9}$			
ACIS-S/HETG: powerlaw						
$F_{\rm x}({\rm ergs~s^{-1}~cm^{-2}})^a$	$92.33^{+1.97}_{-2.56} \times 10^{-12}$	$52.88^{+1.94}_{-2.53} \times 10^{-12}$	$25.73^{+1.38}_{-1.15} \times 10^{-12}$			
$L_{\rm X}({\rm ergss^{-1}})^a$	$29.70^{+0.63}_{-0.82} \times 10^{33}$	$17.01^{+0.62}_{-0.81} \times 10^{33}$	$8.28^{+0.44}_{-0.37} \times 10^{33}$			
$\dot{M}(\mathrm{M}_{\odot}\mathrm{yr}^{-1})^{b}\ldots\ldots$	$4.03^{+0.09}_{-0.11} \times 10^{-9}$	$2.31^{+0.08}_{-0.11} \times 10^{-9}$	$1.12^{+0.06}_{-0.05} \times 10^{-9}$			
ACIS-S/HETG: powerlaw+mekal						
$F_{\rm x}({\rm ergss^{-1}cm^{-2}})^{c}\ldots$	$120.37^{+1.89}_{-3.56} \times 10^{-12}$	$62.90^{+3.07}_{-3.62} \times 10^{-12}$	$55.97^{+1.92}_{-2.67} \times 10^{-12}$			
$L_{\rm X}({\rm ergss^{-1}})^{c}$	$38.72^{+0.60}_{-1.15} \times 10^{33}$	$20.24^{+0.99}_{-1.16} \times 10^{33}$	$18.00^{+0.61}_{-0.86} \times 10^{33}$			
$\dot{M}(\mathrm{M}_{\odot}\mathrm{yr}^{-1})^{b}\ldots\ldots$	$5.25^{+0.08}_{-0.16} \times 10^{-9}$	$2.75^{+0.13}_{-0.16} \times 10^{-9}$	$2.44^{+0.08}_{-0.12} \times 10^{-9}$			

Note. The unabsorbed X-ray fluxes are for the models with the best-fit parameters listed in Tables 2 and 3. "The flux $F_{\rm X}$ derived from an unabsorbed powerlaw over the 0.3–8 keV energy range, and the corresponding luminosity $L_{\rm X}$ at the distance of $D=1.64\,{\rm kpc.}^{b}$ The mass-accretion rate \dot{M} estimated based on the 0.3–8 keV luminosity $L_{\rm X}$, and $M_{\rm WD}=1.25\,{\rm M}_{\odot}$ and $R_{\rm WD}=7.1\times10^{8}\,{\rm cm}$ from Luna et al. (2018). "The flux $F_{\rm X}$ and luminosity $L_{\rm X}$ derived from an unabsorbed powerlaw and mekal model over the 0.3–8 keV energy range ($D=1.64\,{\rm kpc}$).

Table 4 lists the fluxes (F_x) derived from the unabsorbed hard model over the 0.3-8 keV energy range from the time-averaged, low/hard-state, and high/soft-state spectra for both the HRC-S and ACIS-S observations. It also presents their corresponding luminosities (L_x) calculated at the distance of D = 1.64 kpc, together with their mass accretion rates (\dot{M}) calculated by equation (3), and the WD mass and radius from Luna et al. (2018). We obtained source fluxes of $F_x \approx 35 \times 10^{-12}$ and 92×10^{-12} erg cm⁻² s⁻¹ over the 0.3–8 keV energy range from the unabsorbed power-law model fitted to the time-averaged HRC-S and ACIS-S spectra, respectively. Assuming a distance of D = 1.64 kpc, we derived an X-ray luminosities of L_x $\approx 11 \times 10^{33} \, \mathrm{erg \, s^{-1}}$ for the HRC-S time-averaged spectrum. For the ACIS-S data, we estimated $L_x \approx 30 \times 10^{33} \, \mathrm{erg \, s^{-1}}$ at $D = 1.64 \, \mathrm{kpc}$, whereas 44×10^{33} erg s⁻¹ at D = 2 kpc, which is slightly higher than $L_{\rm x} = 31^{+8}_{-7} \times 10^{33} \, {\rm erg \, s^{-1}}$ derived by Luna & Sokoloski (2007) at D $= 2 \,\mathrm{kpc}$.

Our X-ray luminosities estimated at $D = 1.64 \,\mathrm{kpc}$ from the unabsorbed powerlaw model correspond to mass-accretion rates of $\dot{M} \approx 1.5 \times 10^{-9} \, \rm M_{\odot} \, yr^{-1} \, in \, 2015 \, (HRC-S) \, and \, 4 \times 10^{-9} \, \rm M_{\odot} \, yr^{-1} \, in$ 2005 (ACIS-S). They are close to the mass-accretion rate $\dot{M} \approx 1.8 \times 1.8 \times$ $10^{-9} \,\mathrm{M_\odot} \,\mathrm{yr}^{-1}$ estimated at $D=2 \,\mathrm{kpc}$ from a cooling flow model by Luna & Sokoloski (2007). Keeping the hard thermal plasma emission component in the ACIS-S model (powerlaw+mekal), we also derived $\dot{M} \approx 5.3 \times 10^{-9} \,\mathrm{M}_\odot \,\mathrm{yr}^{-1} \,(D/1.64 \,\mathrm{kpc})^2$ for the 2005 observation, which is within mass-accretion rates of $3.7 \times 10^{-9} \, M_{\odot} \, yr^{-1}$ and $6.7 \times 10^{-9} \,\mathrm{M_{\odot} \, yr^{-1}}$ estimated at $D = 2 \,\mathrm{kpc}$ by Luna et al. (2018) from the two separate Suzaku observations of low- and high-brightness epochs, respectively. They also estimated a massaccretion rate of $4.3 \times 10^{-9} \, M_{\odot} \, yr^{-1} from$ the NuSTAR and Swift observations. Luna et al. (2018) pointed out that the mass-accretion rate increases during the brightening event. However, our ACIS-S powerlaw+mekal model yielded $\dot{M} \approx 2.8 \times 10^{-9} \, \mathrm{M_{\odot}} \, \mathrm{yr^{-1}}$ in the low/hard state and $2.4 \times 10^{-9} \,\mathrm{M}_{\odot} \,\mathrm{yr}^{-1}$ in the high/soft state, which do not seem to agree with higher mass-accretion rates when the source was in the high (brighter) state. Additionally, we obtained roughly similar mass-accretion rates for the low/hard- and high/softstate HRC-S observations. We also noticed that the mass-accretion rate derived from the unabsorbed powerlaw model of the HRC-S low/hard-state spectrum was slightly higher than that in the high/soft state (see Table 4). This trend in the HRC-S mass-accretion rates is similar to those deduced from the unabsorbed powerlaw+mekal model of the ACIS-S in the low/hard and high/soft states.

As seen in Table 4, the mass-accretion rates were roughly about $\dot{M} \approx 2.7 \times 10^{-9} \,\mathrm{M}_{\odot} \,\mathrm{yr}^{-1} \,(D/1.64 \,\mathrm{kpc})^2$ or $\dot{M} \approx 4 \times 10^{-9} \,\mathrm{M}_{\odot} \,\mathrm{yr}^{-1}$ $10^{-9} \,\mathrm{M}_{\odot} \,\mathrm{yr}^{-1} \,(D/2.0 \,\mathrm{kpc})^2$ in both the low/hard and high/soft states of the Chandra HRC-S observations (powerlaw) and ACIS-S observation (powerlaw+mekal). This mass-accretion rate agrees with $\dot{M} \approx 4 \times 10^{-9} \,\mathrm{M}_{\odot} \,\mathrm{yr}^{-1} \,(D/2.0 \,\mathrm{kpc})^2$ derived from NuSTAR+Swift and Suzaku low-brightness epoch (Luna et al. 2018). The lower mass-accretion rate of $\dot{M} \approx 1.5 \times 1.5$ $10^{-9} \,\mathrm{M}_{\odot} \,\mathrm{yr}^{-1} \,(D/1.64 \,\mathrm{kpc})^2$ derived from the time-averaged HRC-S spectrum, and the higher mass-accretion rate of $\dot{M} \approx 5.3 \times 10^{-3}$ $10^{-9} \,\mathrm{M_{\odot} \, yr^{-1}} \, (D/1.64 \,\mathrm{kpc})^2$ from the time-averaged ACIS-S spectrum might be related to some variations in the hard band, which were not separated in the mean spectra. We also notice $\dot{M} \approx$ $6.7 \times 10^{-9} \,\mathrm{M_{\odot}} \,\mathrm{yr^{-1}}$ estimated at $D = 2 \,\mathrm{kpc}$ from the Suzaku highbrightness epoch (Luna et al. 2018), which is comparable to the value derived for the time-average ACIS-S observation in 2005 when the source in the hard excess was apparently brighter than the HRC-S observations in 2015. The variation in brightness could be partially related to the absorbing materials within the line of sight that obscure the X-ray source brightness in different epochs, and does not seem to have any strong correlation with the mass-accretion rate.

4.2 Flickering variations

The light curves of the HRC-S/LETG (see Fig. 1) show that the soft bands (*S*: 0.3–4 keV) have variations with larger amplitudes than the hard bands (*H*: 4–8 keV). However, it can be seen in Fig. 2 that the light curves of the ACIS-S/HETG data had variations with similar amplitudes in both the soft and hard bands. We should note that the hard energy band of the source in the ACIS-S observation in 2005

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was much brighter than the HRC-S observation in 2015. We also see that the source exhibits short flickering (brightening) variations on hour timescales without any periodic modulations, which could be related to either rapid outbursts or obscuring absorption materials. These brightening variations appear in the S band of the HRC-S observations in 2015 (red triangles in Fig. 1) and in the S and S bands of the ACIS-S observation in 2005 (see Fig. 2). They are mostly in the high/soft state (red triangles in Figs 3 and 2). As seen in Table 4, the unabsorbed X-ray luminosities S were roughly the same in the low/hard and high/soft states of the HRC-S (powerlaw) and ACIS-S (powerlaw+mekal), so variation in the absorbing material could partially be responsible for the brightening events. We also see that the mass-accretion rates are slightly higher in the low sate, so it does not seems to be a big contributor to the flickering events.

As seen in Tables 2 and 3, the X-ray source was much brighter in the hard band (4–8 keV) when it was in the low/hard states due to higher normalization factors (K_p). However, it is less brighter in the hard band when it was in the high/soft state containing more flickerings, so the brightening might originate from mechanical processes in the accretion disc. A slight increase in the mass-accretion rate might make the X-ray source harder and fainter. Our analysis of the HRC-S and ACIS-S data revealed that the plasma temperature in the low/hard state was higher than in the high/soft state, so the plasma was hotter when the source was fainter. As the brightening events are anticorrelated with the plasma temperatures, they should originate from the outer layers of the accretion disc, so either rapid outbursts or absorbing materials could generate them.

4.3 Origin of the iron lines

The HRC-S and ACIS-S spectra show a strong fluorescent iron K α line at 6.4 keV (see Fig. 5) that could be an indication of either the reflection off an accretion disc or dense clumpy materiel within the line of sight. As seen in Tables 2 and 3, the Fe K α line was twice stronger in the HRC-S time-averaged spectrum compared to the ACIS-S. While the Fe K α line measurements have large uncertainties in the low/hard and high/soft states due to lower count rates, it can be seen that it is probably stronger in the high/soft state than the low/hard state in the HRC-S epoch in 2015, while it is opposite in the ACIS-S epoch. We should note that the HRC-S epoch does not have the same brightness as the ACIS-S. The Fe K α line could be emitted mostly from the pre-shock accreting matter in the HRC-S epoch. As the brightening was higher in the high/soft-state HRC-S events, the fluorescent iron $K\alpha$ emission line could be more intense due to denser clumpy materiel in the outer layers. Nevertheless, we see a stronger Fe K α line in the low/hard-state ACIS-S events compared to its high/soft-state events. A higher accretion rate (see Table 4) and slightly lower absorbing column density in the hard excess (see Table 3) might explain this discrepancy in the Fe K α line.

Similarly, the photo-ionized iron lines (Fe XXV and Fe XXVI) are likely stronger in the HRC-S epoch in 2015 than the ACIS-S epoch in 2005. However, we should also consider high uncertainties in the HRC-S measurements. It is also possible that the hard excess of the source in the HRC-S epoch was harder, so the hard radiation produced the stronger Fe XXV and Fe XXVI lines. The unabsorbed X-ray luminosities measured over the 0.3–8 keV energy range (see the power-law models presented in Table 4) suggest that the *hard* excess of the X-ray source was at least three times luminous in the ACIS-S epoch than the HRC-S epoch. However, the power-law photon index Γ was approximately the same in different *Chandra* observations in

2005 and 2015 (see Tables 2 and 3). We also found extremely weak constraints (see Figs A2–A5) on the Fe XXV and Fe XXVI lines in the low/hard and high/soft states of the HRC-S and ACIS-S epochs (due to the low count rate), so we could not interpret them according to different states.

4.4 Comparison of ACIS-S and HRC-S epochs

As seen in Figs 1–4, the hard excess of the source was brighter and has a higher X-ray luminosity (see Table 4) in 2005 compared to 2015. We should note that the ACIS-S/HETG effective area dramatically drops at energies below 1 keV, so it cannot detect any thermal plasma components in the soft band (0.3–4 keV). However, the HRC-S/LETG instrument has more effective area in the soft band than the hard band, so it provides fewer details about possible thermal plasma components in the hard band (4–8 keV). Although the HRC-S/LETG instrument has a significant background noise, it has a better sensitivity than the ACIS-S/LETG to detect any plasma emission below 2 keV, so the HRC-S/LETG observation is expected to reveal the thermal emission in the soft band.

As seen in Tables 2 and 3, our thermal plasma mekal modelling of the Chandra observations of RT Cru suggests two plasma temperatures of $kT \sim 1.3$ and 9.6 keV in the HRC-S and ACIS-S time-averaged spectra, respectively. Moreover, we obtained $kT \sim$ 1.1 (HRC-S) and 10.3 keV (ACIS-S) from the apec model fitted to the time-averaged spectra. Our spectral analyses imply that the soft thermal plasma emission component with $kT \sim 1.3$ was obscured by some dense clumpy materials with a column density of $N_{\rm H, mk} \sim$ $76 \times 10^{22} \,\mathrm{cm^{-2}}$ in the HRC-S/LETG epoch (2015) when the hard excess of the source was fainter than the 2005 epoch. However, it seems that the hard thermal plasma emission component with kT ~ 10 was obscured by less dense absorbing materials with $N_{\rm H.\,mk}$ $\sim 12 \times 10^{22} \, \mathrm{cm}^{-2}$ in the ACIS-S/HETG epoch (2005) when the source was brighter in the hard band. We notice that the fitted powerlaw model has a column density of $N_{
m H,\,p}\sim 5\times 10^{22}\,{
m cm}^{-2}$ for the HRC-S/LETG (2015), which is significantly lower than $N_{\rm H, p}$ $\sim 100 \times 10^{22} \, \mathrm{cm}^{-2}$ derived for the ACIS-S/HETG time-averaged spectrum (2005).

We also fitted the thermal plasma model to the low/hard-state and high/soft-state events, which were classified based on the HR diagrams shown in Figs 3 and 4 under the criteria defined in Section 3.2. It can be seen in Tables 2 and 3 that the plasma temperature was higher in the low/hard state of both the HRC-S (2015) and ACIS-S (2005). Fitting mekal and apec to the low/hard-state HRC-S spectrum yields plasma temperatures of kT = 1.5 and 1.3 keV, respectively, which are slightly higher than those derived from the time-averaged HRC-S spectrum. For the low/hard-state ACIS-S spectrum, we also derived $kT = 46^{+13}_{-17} \,\text{keV}$ (mekal) and $kT = 51^{--}_{-42} \,\text{keV}$ (apec), which are comparable to the maximum post-shock temperature of $kT_{\text{max}} = 53 \pm 4 \,\text{keV}$ derived by Luna et al. (2018) from the Suzaku and Suz

The power-law indexes of the hard band (4–8 keV) were $\Gamma=1.7$ in 2015 and $\Gamma=1.8$ in 2005, so they were roughly similar in the time-averaged spectra. The fluorescent iron emission line at 6.4 keV, which could be emitted from either reflection off an accretion disc or dense absorbing material, was measured to be twice stronger in the HRC-S time-averaged spectrum compared to the ACIS-S. Stronger Fe K α line might be an indication of higher neutral dense clumps. Interestingly, the soft thermal plasma emission component ($kT\sim1.3$) identified in the HRC-S is likely obscured by dense clumpy materials.

By contrast, the hard thermal plasma emission component ($kT \sim 10$) detected in the ACIS-S is likely absorbed by less dense obscuring materials, when the Fe K α line was by a factor of 2 lower than that measured in the HRC-S. Nevertheless, this is in contradiction to absorbing column densities derived from the absorbed powerlaw model (see Tables 2 and 3). It is possible that both the soft ($kT \sim 1.3$) and hard ($kT \sim 10$) thermal plasma emission components are emitted from outer layers of the accretion disc having dense clumps, which are not the same material blocking the hard excess in the powerlaw models.

5 SUMMARY AND CONCLUSION

To summarize, we conducted a detail spectral analysis of the hard X-ray emitting symbiotic system RT Cru observed using the *Chandra* HRC-S/LETG for a total exposure of 79 ks in 2015, and ACIS-S/HETG for 49 ks in 2005. We have modelled the hard excess above 4 keV with a power-law model partially covered by a local absorber, in addition to the Fe K α , Fe XXV, and Fe XXVI lines using three Gaussian functions. We have extended our spectral analysis to the soft excess below 4 keV by including a thermal plasma model fully covered by another local absorber. Additionally, we applied the same modelling procedures to the spectra generated from events separated into the low/hard and high/soft states according to the HR diagrams. Our key findings obtained from *Chandra* HRC-S/LETG and ACIS-S/HETG are as follows:

- (1) Our hardness ratio analysis of the light curves of the soft (S: 0.3–4 keV) and hard (H: 4–8 keV) bands revealed two distinct states (see Figs 3 and 4), namely *low/hard* and *high/soft* states. The X-ray source shows aperiodic flickering variations mostly from the soft excess in the HRC-S epoch (see Fig. 1), but also from the hard excess in the ACIS-S epoch (see Fig. 2). We found an anticorrelation relation between the hardness ratio (H/S) and total brightness (H+S) in both the HRC-S and ACIS-S epochs, implying that the X-ray source was fainter when it was harder, and vice versa.
- (2) The time-averaged HRC-S/LETG and ACIS-S/HETG spectra likely have the same hard X-ray continuum above 4 keV described by a powerlaw model with a photon index of about $\Gamma \sim 1.7-1.8$ over the 4–8 keV energy range. While the X-ray source was fainter in the HRC-S epoch in 2015, its K α fluorescent iron emission line at 6.4 keV is twice as brighter compared to the ACIS-S epoch in 2005. A higher value of the Fe K α line may be an indication for a denser neutral absorber located in the outer layers. The soft excess is more obscured by heavily dense absorbing materials in the HRC-S epoch, while we have no knowledge about the physical condition of the soft band in the ACIS-S epoch. By contrast, the hard excess is less obscured in the HRC-S, while it is heavily absorbed in the ACIS-S epoch (see Tables 2 and 3).
- (3) In the low/hard state when the X-ray source was fainter and harder, the spectra were fitted by a power-law phenomenological model over 4–8 keV having photon indexes of $\Gamma\sim2.4$ and 2 in the HRC-S and ACIS-S epochs, respectively. In the high/soft state when the X-ray source was brighter and softer, the spectra were fitted by lower power-law indexes $\Gamma\sim1.7$ (HRC-S) and 0.9 (ACIS-S) over the 4–8 keV energy range. This is in contrast to the photon index behaviour is typically seen in the low/hard and high/soft states of X-ray binary over 0.3–8 keV. However, we derived roughly the same X-ray luminosities from the unabsorbed powerlaw model for the low/hard and high/soft states in the HRC-S (see Table 4), and the similar X-ray luminosities from the unabsorbed

powerlaw+mekal model for the low/hard and high/soft states in the ACIS-S. Interestingly, these unabsorbed hard X-ray luminosities are very close to $\sim 60 \times 10^{-12}$ erg s⁻¹ cm⁻².

- (4) The thermal emissions of the time-averaged HRC-S/LETG and ACIS-S/HETG spectra were well reproduced by thermal plasma mekal models with $kT \sim 1.3$ and 9.6 keV, respectively. For the HRC-S/LETG, we also derived $kT \sim 1.5$ keV in the low/hard state (fainter and harder) and $kT \sim 0.6$ keV in the high/soft state (brighter and softer). For the ACIS-S/HETG, we estimated $kT \sim 46$ and 4 keV in the low/hard and high/soft states, respectively.
- (5) From the unabsorbed powerlaw model fitted to the HRC-S time-averaged spectrum, we derived a mass accretion rate of $\dot{M}\sim 1.5\times 10^{-9}\,\rm M_\odot\,yr^{-1}$ (at $D=1.64\,\rm kpc$), whereas for the ACIS-S time-averaged spectrum, we obtained $\dot{M}\sim 4\times 10^{-9}\,\rm M_\odot\,yr^{-1}$ from the unabsorbed powerlaw model and $\dot{M}\sim 5.3\times 10^{-9}\,\rm M_\odot\,yr^{-1}$ from the unabsorbed powerlaw+mekal model. However, we obtained roughly $\dot{M}\sim 2.7\times 10^{-9}\,\rm M_\odot\,yr^{-1}$ for low/hard and high/soft states of the HRC-S (powerlaw) and the ACIS-S (powerlaw+mekal), so the discrepancy between the time-averaged HRC-S and ACIS-S might be related to some variations in the hard band of the ACIS-S and strong soft flickerings in the HRC-S, which were not separated from each other in the time-averaged spectra.

In conclusion, our Bayesian low-count X-ray spectral analysis of the Chandra HRC-S/LETG and ACIS-S/HETG observations provided the first evidence for the soft thermal plasma emission component ($kT \sim 1.3 \, \text{keV}$), in addition to the reconfirmation of the hard thermal plasma emission component ($kT \sim 10 \,\mathrm{keV}$) previously identified. This soft emission component is possibly largely obscured by highly dense materials ($N_{\rm H, mk} > 5 \times 10^{23} \, {\rm cm}^{-2}$) within the line of sight. Future observations by Chandra ACIS-S/LETG with a significantly longer exposure time will be able to verify this soft thermal plasma emission. In particular, the Arcus mission (Smith et al. 2016), recently admitted to Phase A study, would offer a more effective area at energies below 1 keV, which would allow us to reaffirm its presence in the soft excess. Interestingly, some other hard X-ray emitting symbiotics have also been found to contain two distinct (soft and hard) thermal plasma emission components, namely CH Cyg (kT = 0.2, 0.7 and 7.3 keV; Ezuka, Ishida & Makino 1998), MWC 560 (kT = 0.18 and 11.26 keV; Stute & Sahai 2009), and SS73 17 (kT = 1.12 and 9.9 keV; Eze et al. 2010). In particular, jets have been detected in CH Cyg (Corradi et al. 2001; Sokoloski & Kenyon 2003; Galloway & Sokoloski 2004; Karovska et al. 2007, 2010) and MWC 560 (Tomov et al. 1990, 1992; Schmid et al. 2001; Lucy, Knigge & Sokoloski 2018), while Eze et al. (2010) also suggested a possible unseen jet in SS73 17. Although the soft thermal plasma emission component could be associated with a jet in the symbiotic system, Stute & Sahai (2009) pointed out that the 0.8-1 keV soft thermal component can also be emitted from shocks (with velocities of $\sim 1000 \,\mathrm{km}\,\mathrm{s}^{-1}$) created by colliding winds of accreting flows. However, we have not been able to find clear evidence of a jet in RT Cru through these data.

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DATA AVAILABILITY

The observational raw data underlying this article are available in the *Chandra* Data Archive (CDA) at https://cda.harvard.edu/chaser/, and the processed data will be shared on reasonable request to the corresponding author.

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SUPPORTING INFORMATION

Supplementary data are available at MNRAS online.

Appendix A. Bayesian Low-Count X-ray Spectral Analysis The following figures are available for the electronic edition of this article:

Figures A1–A5. The same as Fig. 6, but for the HRC-S/LETG time-averaged spectrum, and the ACIS-S/HETG and HRC-S/LETG *low/hard-* and *high/soft-*state spectra, respectively.

Figures A6–A9. The same as Fig. 8, but for the HRC-S/LETG *high/soft*-state spectrum, the ACIS-S/HETG time-averaged spectrum, and the ACIS-S/HETG *low/hard*- and *high/soft*-state spectra, respectively.

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